

UNIVERSITY SUPPLEMENTARY/SPECIAL EXAMINATIONS

2022/2023 ACADEMIC YEAR YEAR THREE SEMESTER TWO EXAMINATIONS FOR THE BACHELORS DEGREE

COMPUTER SCIENCE

COURSE CODE: CSC 354E

COURSE TITLE: SIGNALS AND SYSTEMS II

DATE: 16/08/2023 TIME: 8.00AM-10AM

INSTRUCTIONS TO CANDIDATES

ANSWER QUESTION ONE AND ANY OTHER TWO (2) QUESTIONS

QUESTION ONE (30 MARKS COMPULSORY)

- a) Given that $x[n] = \delta[n-3]$, find the Z transform X[Z] [3marks]
- b) Explain the special feature of z-transforms which is of interest in discrete signals [3marks]
- c) Given that $L(e^t) = \frac{1}{(s-1)}$, find $L(e^{3t})$ [4marks]
- d) Outline FOUR Laplace Transform properties for Laplace Transform [8marks]
- e) Find Laplace Transform of
 - i) f(t)=3 [2marks]
 - ii) $f(t) = 2 + 3e^{2t}$ [2marks]
- f) State two useful applications of z-transforms in LTI systems [2marks]
- g) Outline two useful properties of z-transforms [6marks]

QUESTION TWO (20 MARKS)

- a) Find the Laplace Transform of the following signals
 - i) Unit impulse, f(t) = 1 [2marks]
 - ii) $f(t) = e^t$ [3marks]
- b) Find the inverse Laplace of $F(s) = \frac{2}{s^2 + 3s + 2}$ [9marks]
- c) Find the Laplace transforms of the following functions
 - i) $f(t) = e^{3t} (t^3 + 3t 3)$ [3marks]
 - ii) $f(t) = t^3 + 3t 3$ [3marks]

QUESTION THREE (20 MARKS)

- a) Find the Laplace transform of the following signals
 - i) $f(t) = 3\delta(t) 2e^t$ [5marks]
 - ii) $f(t) = t^3$ [3marks]
- b) Find the inverse Laplace transform of $F(s) = \frac{2}{s+4}$ [4marks]
- c) Find the output of the two-tap FIR given in figure 3c [8marks]

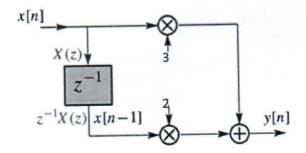


Figure 3c

QUESTION FOUR (20 MARKS)

- a) Given that the Laplace transform of $f(t) = \cos \omega t$ is $F(s) = \frac{s}{s^2 + \omega^2}$, find the Laplace of the following signals
 - i. $f(t) = \cos 4t$
 - ii. $f(t)=2\cos 3t$

[4marks]

b) Find the inverse Laplace transform of $F(s) = \frac{5}{s^2 - 9^2}$

[6marks]

c) Given that the input and the impulse response of a system are

$$x[n] = \delta[n] - 2\delta[n-2] + 5\delta[n-3]$$

$$h[n] = 3\delta[n] + \delta[n-1] + 2\delta[n-2]$$

Find the output of the system

[6marks]

d) Find the input-output equation for the system shown in figure 4d.

[4marks]

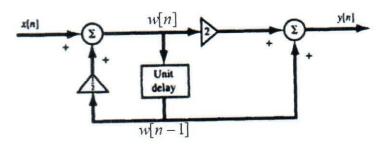


Figure 4d

QUESTION FIVE (20 MARKS)

a) Find the inverse Laplace Transform of the following transforms

I.
$$F(s) = \frac{3!}{s^4} + 5\frac{1}{s^2} - 2\frac{1}{s}$$

[3marks]

II.
$$F(s) = \frac{3!}{(s-2)^4} + 5\frac{1}{(s-2)^2} - 2\frac{1}{s-2}$$

[3marks]

b) Solve the initial value problem

$$y'-3y'-10y=2$$
,

$$y(0) = 1, y'(0) = 2$$

[7marks]

- c) Consider the discrete-time system shown in figure 5c.
 - i) Write down a difference equation that relates the output y[n] and the input x[n].[3marks]

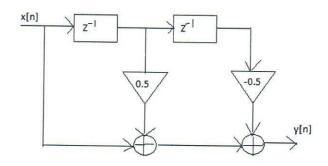


Figure 5c

ii) Given that

$$Y(z) = 1 + 2Z^{-1} - Z^{-2} - 2Z^{-2}$$
 and

$$X(z) = 1 - Z^{-1}$$

Find the transfer function h[n] of the system.

[4marks]