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**UNIVERSITY EXAMINATIONS  
2022/2023 ACADEMIC YEAR  
SECOND YEAR SECOND SEMESTER  
MAIN EXAMINATION**

**FOR THE DEGREE OF BACHELOR OF SCIENCE  
(RENEWABLE ENERGY)**

**COURSE CODE: MA 252**

**COURSE TITLE: ENGINEERING MATHEMATICS II**

**DATE:**

**TIME:**

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**INSTRUCTIONS TO CANDIDATES**

Answer Question One and Any other TWO Questions

**TIME: 2 Hours**

This Paper Consists of 3 Printed Pages. Please Turn Over.

**QUESTION ONE (30 MARKS)**

(a) Differentiate between thermodynamics and adiabatic process (2marks)  
in relation to heat.

i) In a adiabatic expansion of a gas,  $C_v \frac{dP}{P} = -C_p \frac{dV}{V}$ , where  $C_p$  and  $C_v$  are constants. Given  $n = \frac{C_p}{C_v}$  show that  $PV^n = \text{Constant}$  using method of separation of variables (3 marks)

(b) Define the term a phasor hence determine a pair of phasors that can be used to represent the following voltage

$$V = 16\cos 4t \quad (2 \text{ marks})$$

(c) For R-C determine the resistance and series inductance for the following assuming the frequency of 100Hz (4marks)

i)  $(5 + i6)\Omega$

ii)  $-i30\Omega$

(d) A production company for renewable energy has 30 similar solar powered machines. The number of breakdowns on each machines average 0.05 per week. Determine probabilities of having less than 3 machines breaking down in any week (3marks)

(e) Consider a function  $g(z) = z^2$  write in terms of  $r$  and  $\theta$  in modulus

Argument form (3 marks)

(f) Convert  $f_r(x) = 10\cos x + 12\sin x$  into complex form ( $f_c(x)$ ) and state the Fourier coefficients. (4 marks)

(g) A hydroelectric power was laid in a gradient defined by an engineer a

$g(x, y, z) = x^2 z^2 \sin(3y)$ . Find the gradient of the function using the definition of gradient. (3marks)

(h)i) Use the line integral to compute work done by a force

$\vec{v} = (2y + 2)\tilde{i} + (xz)\tilde{j} + (yz - x)\tilde{k}$ . When it moves a particle from the point

(0, 0, 0) to the point (4, 2, 2) along the curve  $x = 4t^2, y = t$ . (4marks)

(ii) State stokes theorem. (2marks)

**QUESTION TWO (20 MARKS)**

(a) Consider  $f(a) = a^2$  evaluate and show that the function  $f(a) = a^2$  is differentiable at every point in region  $\mathbb{R}$ .

(10marks)

(b) Find the Laurent series of the function  $f(a) = \frac{1}{(a-1)(a-2)}$  at  $1 < |a| < 2$ .

(10marks)

**QUESTION THREE (20 MARKS)**

(a). State two assumptions that describe the flow of heat in thermally conducting and waves in ocean (2marks)

(b). Find the solution of the initial boundary value problem for the heat equation

$u_{xx} = \alpha^2 u_t$  Satisfying the following initial boundary conditions

$$\begin{cases} u_x(0, t) = 0, \\ u_x(l, t) = 0 \end{cases} \quad 0 \leq t < \infty \quad \text{and} \quad u(x, 0) = \sin \frac{\pi x}{l}, \quad 0 \leq x \leq \pi \quad (10\text{marks})$$

(c). Derive the greens theorem in relation to vectors

(8marks)

**QUESTION FOUR (20 MARKS)**

(a) Given  $\vec{V} = x^2 z \vec{i} - 2y^3 z^2 \vec{j} + xy^2 z \vec{k}$ , Find  $\nabla \cdot \vec{V}$  at  $(1, -1, 1)$  (6marks)

(b) Find  $\text{Curl } \vec{V}$  (6marks)

(c) Consider a closed surface in space  $x, y, z$  enclosing a volume  $V$  as  $\mathbf{B} = 45x^2y$  bounded by the planes  $4x + 2y + z = 8$ ,  $x = 0$ ,  $y = 0$ ,  $z = 0$ . Evaluate (8marks)

**QUESTION FIVE (20 MARKS)**

(a) Use the Laplace transform method to solve the differential equation  $2y'' + 5y' - 3y = 0$  . Given that  $x = 0$ ,  $y = 4$  and  $y' = 9$ . (10marks)

(b) The current flowing in an electrical circuit is given by the differential equation  $Ri + L \left\{ \frac{di}{dt} \right\} = E$ , Where  $E$ ,  $L$  and  $R$  are constants. Use the above method to Solve the equation for current  $i$  given that  $t = 0$  and  $i = 0$ . (10marks)